

Simulation of an Electrostatically Driven Microinjector Pump

**Gopi C. Krishnan, John W. Daily and
James Nabity**

**Center for Combustion and Environmental
Research**

**Department of Mechanical Engineering
University of Colorado at Boulder**



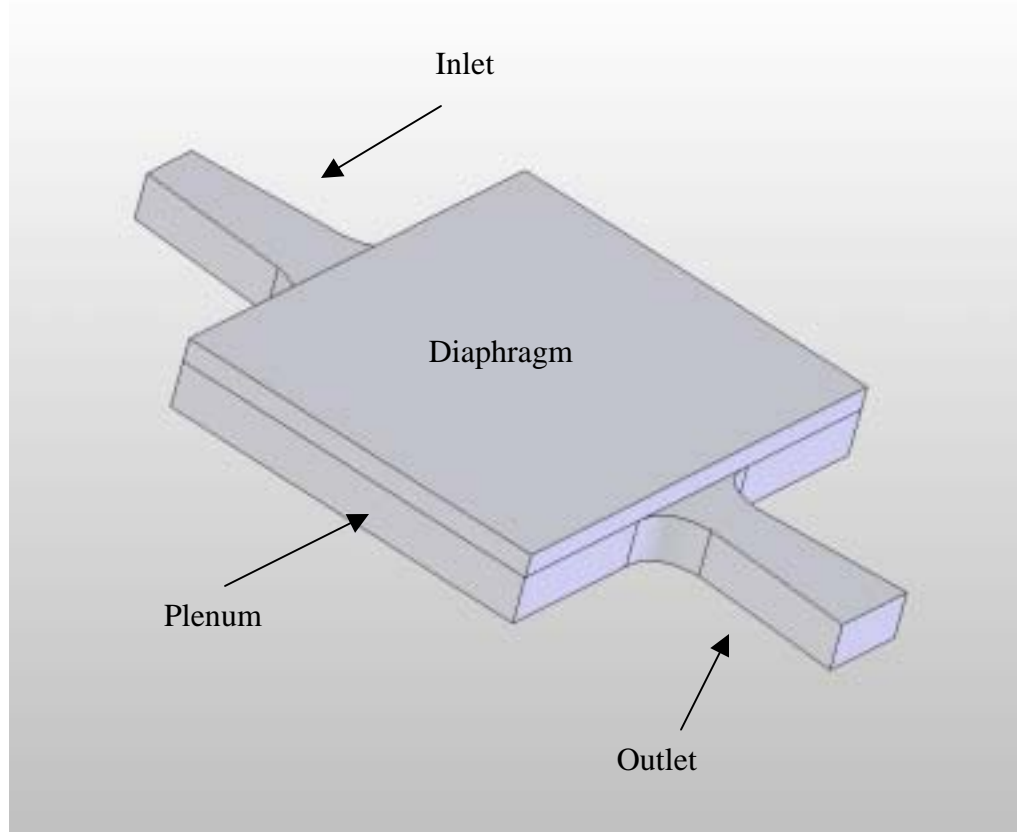
Acknowledgements

- Support for the simulations is from the U.S. Air Force Office of Scientific Research, Program Officer Dr. Mitat Birkin. Award no. F49620-02-1-0133.
- Support for the design and fabrication effort is from the Office of Naval Research, Program Monitor Dr. Chris Brophy. Award to TDA Resaerch Inc. SBIR Phase II Contract no. N00014-01-C-0457. University of Colorado work performed under a subcontract to TDA Research.
- (Design details proprietary, so don't ask! Have injector will sell!)

Motivation

- Goal is to develop fuel injection suitable for Pulsed Detonation Engine (PDE).
- Very small droplet sizes required to initiate detonation $< 3 \mu\text{m}$.
- Exploring use of micro and meso scale technology based on inkjet experience.
- Have developed designs and fabrication methods and are about to start testing.

Model Pump with Passive Valves



Works because
flow resistance
is less in outlet
direction

Previous Work

- Numerous workers have studied micro pumps because of plethora of applications:
 - Woias P., “Micropumps – summarizing the first two decades, Microfluidics and BioMEMS,” Proc. Of SPIE Vol. 4560, 39-52 (2001).
- Of particular interest to us is the work of Olsson:
 - Olsson A., G. Stemme and E. Stemme, “A valve-less planar fluid pump with two pump chambers,” *Sensors Actuators A47*, 549–556 (1995) (And more ...)

Simple Relationships

- Electrostatic Force

$$P = \frac{\epsilon_0 V_{app}^2}{g^2}$$

- Static Deflection

$$y_{\max} = \frac{3P(m^2 - 1)L^4}{16\pi Em^2 t}$$

- Natural Frequency

$$f_1 = \frac{13.49}{2\pi L^2} \sqrt{\frac{D}{\rho t}} \quad D = \frac{Et^3}{12(1-\nu^2)} \quad \frac{f_{1fluid}}{f_{1vac}} = \frac{1}{\left(1 + \frac{A_p}{M_p}\right)^{1/2}}$$

Simple Relations

- Pressure Drop (Nozzle/Diffuser)

$$\Delta p_{N,D} = K_{N,D} \rho \frac{V^2}{2} \quad \eta = \frac{K_N}{K_D}$$

- Net Flow Rate

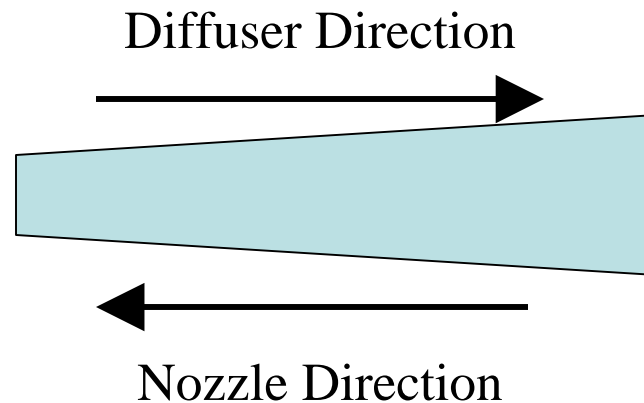
$$Q_p = \frac{V_0 \omega}{\pi} \left(\frac{\eta^{1/2} - 1}{\eta^{1/2} + 1} \right)$$

- Question: How well do these work?

Numerical Methods

- ANSYS Multi-physics finite element code is used to carry out simulation:
 - Weak sequential algorithm to couple structural and fluid dynamics,
 - Arbitrary Lagrangian-Eulerian formulation solves for the fluid flow with moving boundaries,
 - Fluid dynamics is solved using ANSYS FLOTRAN (Flow treated as incompressible.)

Modeled Passive Valve Geometry (Steady-state 2-D Simulation)

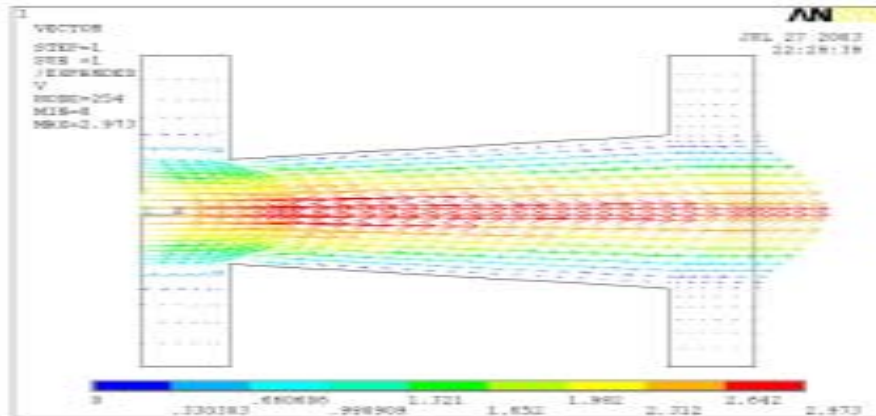


$$L = 1 \mu\text{m}$$

$$w_{\text{outlet}} = 250 \text{ mm}$$

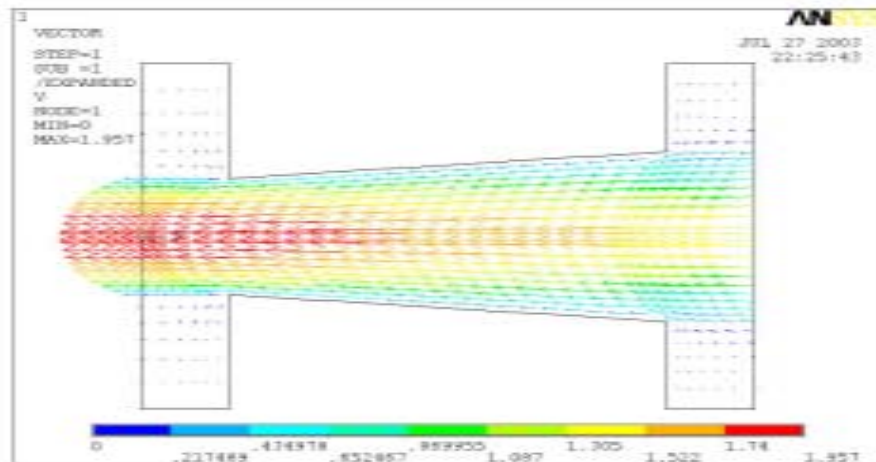
$$\alpha = 5 \text{ degrees}$$

Passive Valve Results



Diffuser Direction

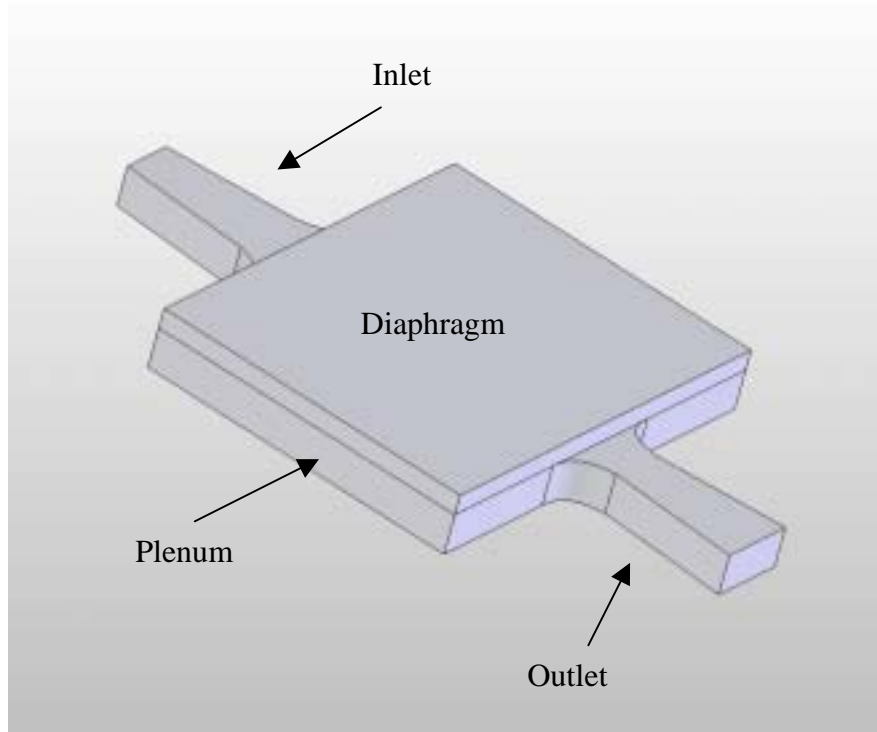
$$Q_D/Q_N \sim 2.2$$



Nozzle Direction

Modeled Pump Geometry

Time Dependent 3-D Simulation



$$L_{\text{diaph}} = 1 \text{ mm}$$

$$t_{\text{diaph}} = 50 \text{ } \mu\text{m}$$

$$t_{\text{plenum}} = 100 \text{ } \mu\text{m}$$

$$t_{\text{passages}} = 100 \text{ } \mu\text{m}$$

$$L_{\text{passages}} = 0.33 \text{ mm}$$

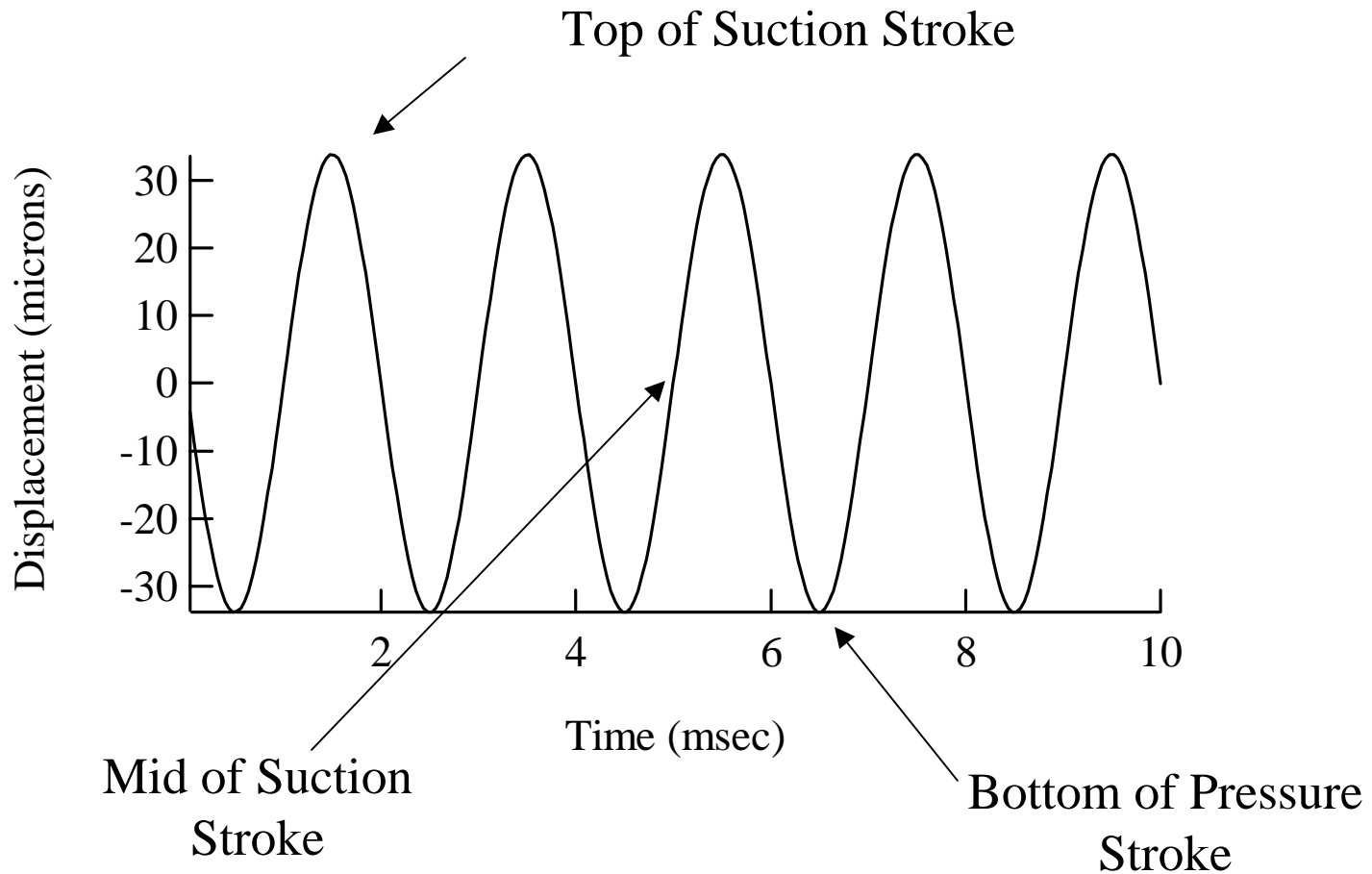
$$W_{\text{inpassages}} = 66.7 \text{ } \mu\text{m}$$

$$\alpha_{\text{valve}} = 5 \text{ degrees}$$

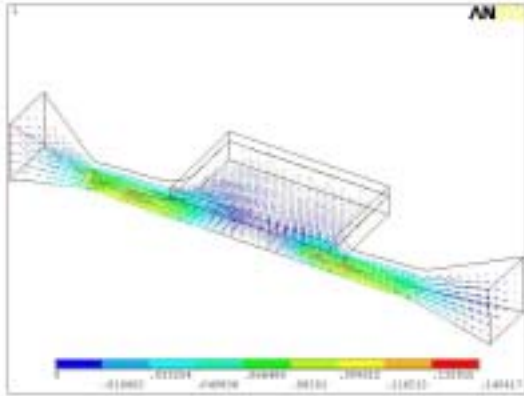
Simulation uses vertical symmetry plane

Calculations for 100-900 Hz

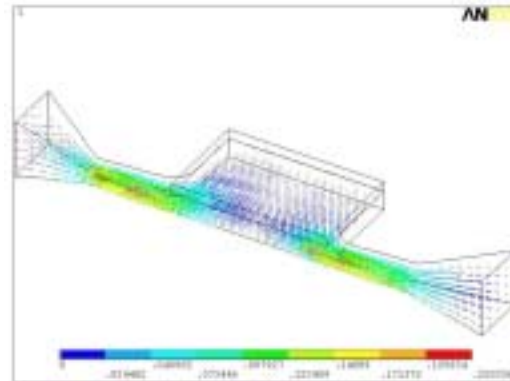
Displacement 500 Hz



Flow Field

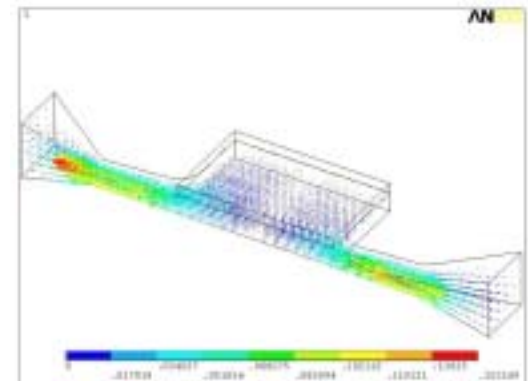


Top of Suction
Stroke

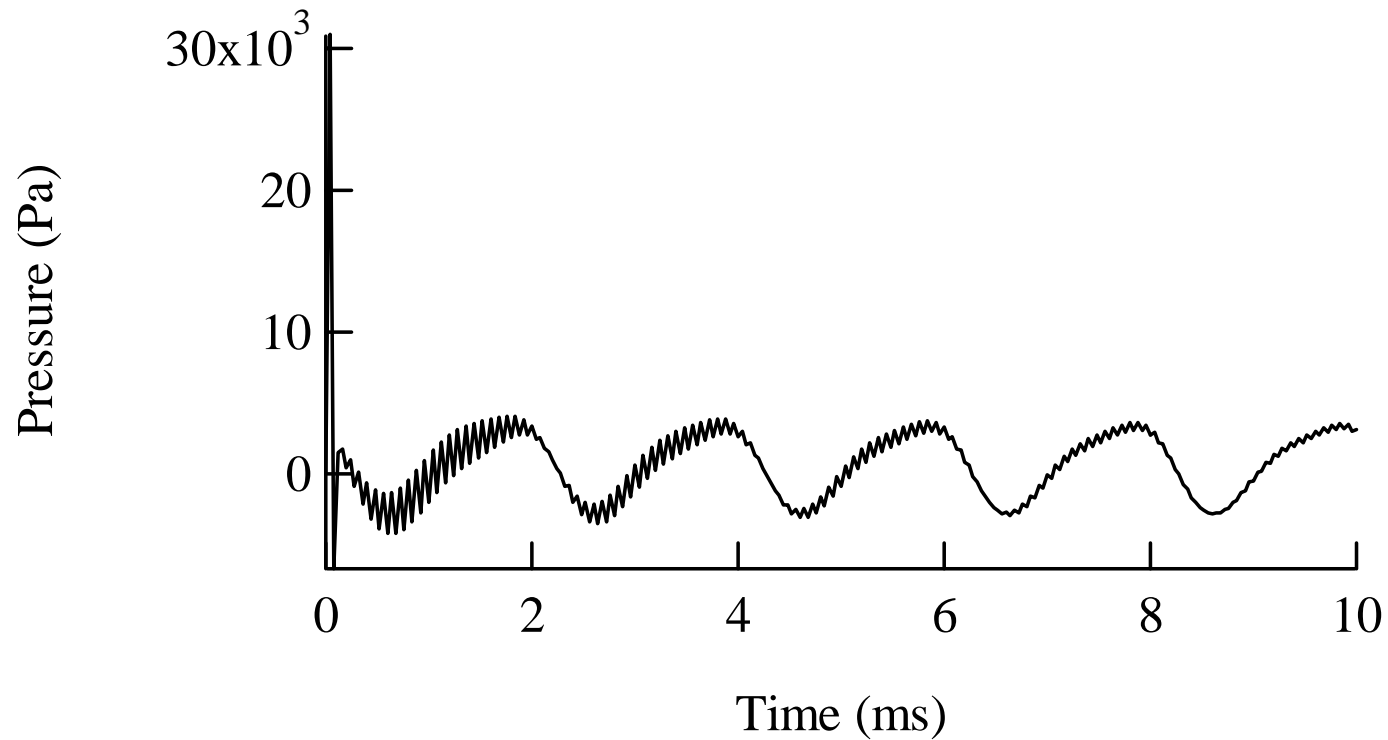


Mid of Suction
Stroke

Bottom of Pressure
Stroke



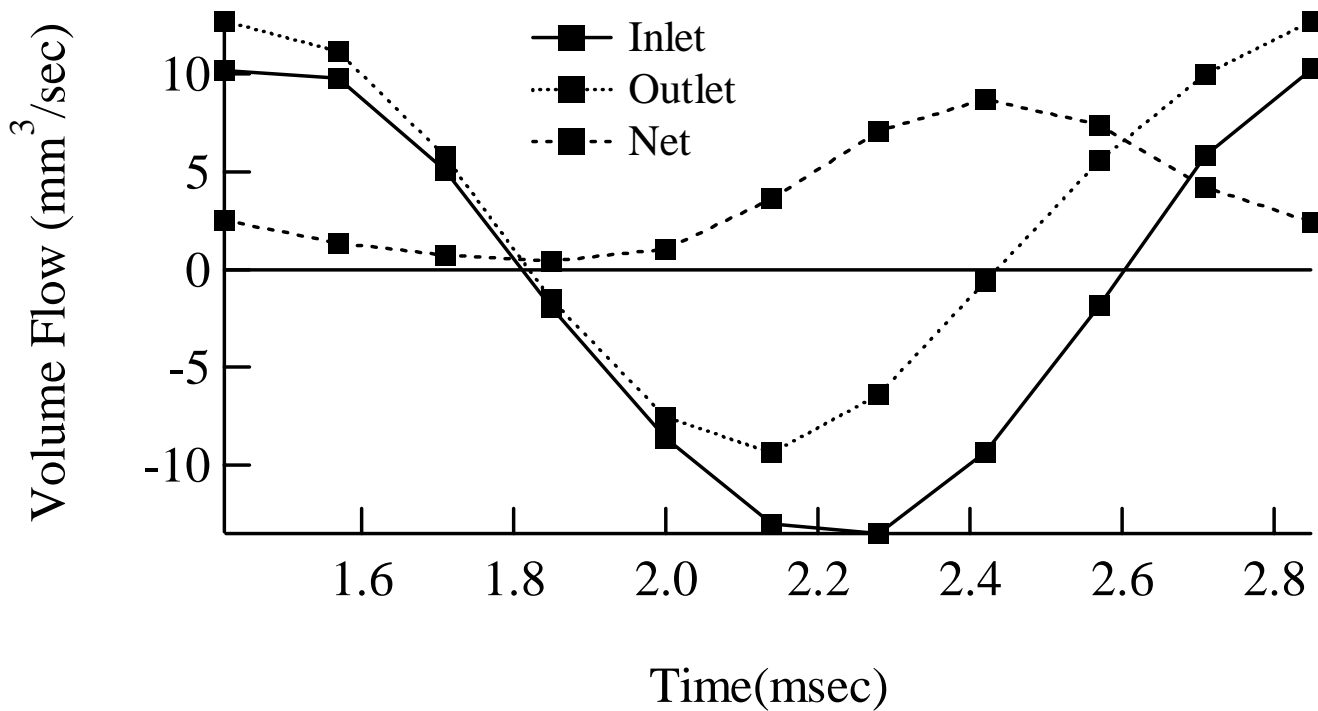
Pressure at Diaphragm Center 500 Hz



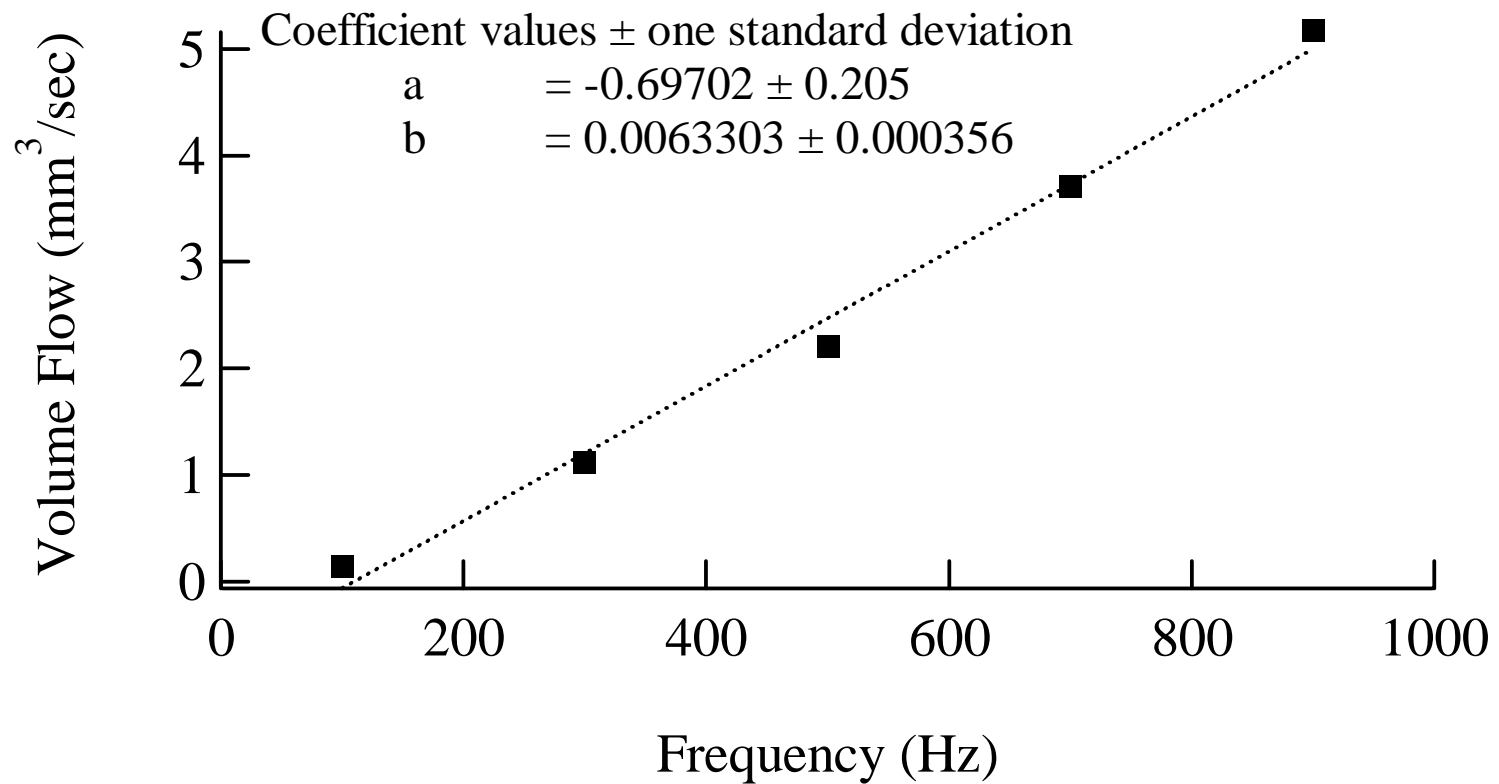
(Compare to ~ 30 MPa applied pressure)

Flow Rates

700 Hz



Net Flow Rate



Discussion

- Net flow generated!
- Olsson relationship predicts linear flow rate increase with frequency when V_0 constant as we observe.
- Olsson relationship does not predict offset observed in their experiments and our simulation.

Discussion

- Fitting Olsson relationship suggests effective $\eta \cong 1.36$ which is smaller than steady calculations predict.
- Differences likely due to complexity of unsteady fluid dynamics.
- Work is needed to optimize passive valving.

Conclusions

- ANSYS code seems to have successfully to simulated valves and pump. (Proof will be in pudding of testing.)
- Flow is somewhat complex, but simple relations can guide design efforts.
- Future work on valve optimization, wider range of operating conditions, exploring designs where diaphragm resonance is approached (meso-scale), and simulating full injector.